



# MODELING OF SUBGRID-SCALE MIXING IN LARGE-EDDY SIMULATION OF SHALLOW CONVECTION

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# Motivation



Shallow convective  
clouds are strongly  
diluted by entrainment

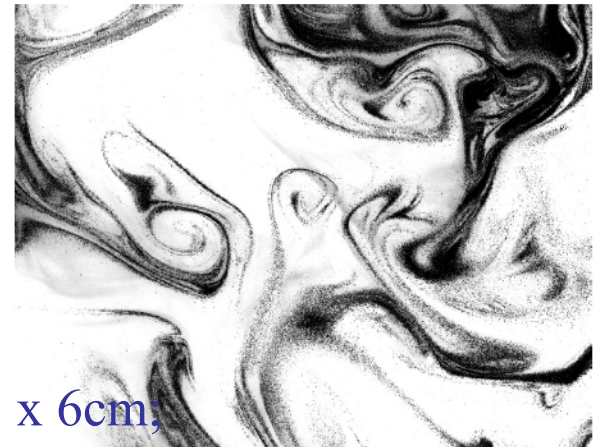
# Overview

For atmospheric LES models, subgrid-scale mixing should cover wide range of situations:

- from extremely inhomogeneous at scales close to model gridlength,
- to homogeneous at scales close to the Kolmogorov scale (typically around 1 mm).



domain size  $\sim 64\text{cm} \times 64\text{cm}$ ;  
*Andrejczuk et al. JAS 2006*



physical area  $\sim 9\text{cm} \times 6\text{cm}$ ;  
*Malinowski et al. NJP 2008*

# Description of model

- The Eulerian version of 3D anelastic semi-Lagrangian-Eulerian model EULAG (Smolarkiewicz et al.).
- Two versions of 1-moment microphysics were used (predicting mixing ratios only):
  - traditional bulk microphysics
  - modified bulk microphysics with additional parameter  $\lambda$  to describe turbulent mixing.

# Bulk microphysics

- Condensation rate  $C$  is defined by constraints that the cloud water can exist only in saturated condition and the supersaturation is not allowed.
- In the bulk model,  $C$  is derived by saturation adjustment after calculation of advection and eddy diffusion -  $C^{sa}$

# Bulk microphysics

Instantaneous adjustment is questionable for the cloud-environment mixing...

This is because microscale homogenization occurs at scales around 1 cm and smaller!

# Possible approaches

- Simple approach: a subgrid scheme based on Broadwell and Breidenthal (JFM 1982) scale collapse model (Grabowski 2007);
- Sophisticated approach: embedding Kerstein's Linear Eddy Model (LEM) in each LES gridbox ("One-Dimensional Turbulence", ODT; Steve Krueger, U. of Utah).

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# $\lambda$ approach

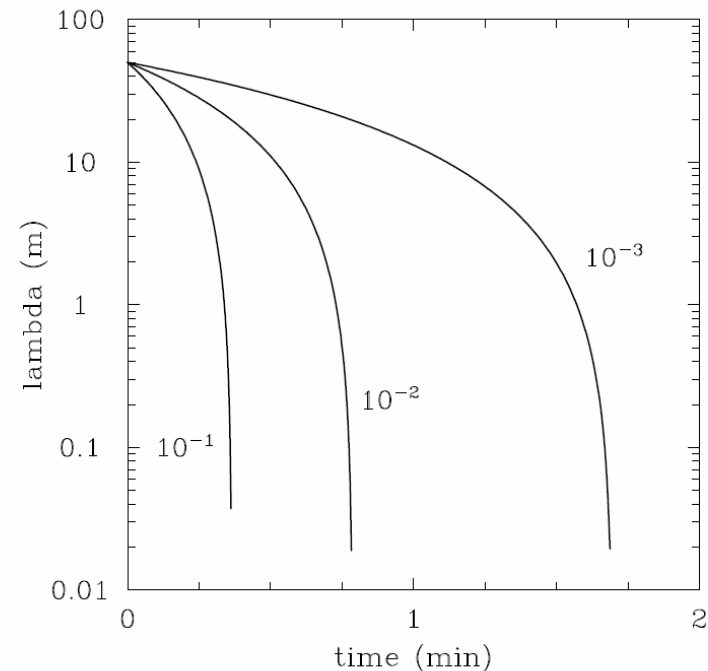
To represent the chain of events characterizing turbulent mixing, Grabowski (JAS 2007) introduced an additional model variable.

spatial scale  $\lambda$  of the cloud filaments during turbulent mixing

$$\frac{d\lambda}{dt} = -\alpha\epsilon^{1/3}\lambda^{1/3}$$

$\epsilon$  - dissipation rate of TKE

(Broadwell and Breidenthal 1982),



# Application of the $\lambda$ equation into model

$$\frac{\partial \lambda}{\partial t} + \frac{1}{\rho_o} \nabla \cdot (\rho_o \mathbf{u} \lambda) = -\alpha \epsilon^{1/3} \lambda^{1/3} + S_\lambda + D_\lambda$$

$\lambda$  has to be between two scales:  $\lambda_0 \leq \lambda \leq \Lambda$ ;

$\Lambda$  is the model gridlength;  $\lambda_0$  is the homogenization scale;  
say,  $\lambda_0 = 1$  cm.

$S_\lambda$  - ensures transitions between cloud-free and cloudy gridboxes (initial condensation) or between inhomogeneous to homogeneous cloudy volume

$D_\lambda$  - subgrid transport term

# Evaporation

Saturation adjustment is delayed until the gridbox can be assumed homogenized:

$$\lambda = \Lambda \text{ or } \lambda \leq \lambda_0 \quad C = C^{\text{sa}} \quad (\text{saturation adjustment})$$

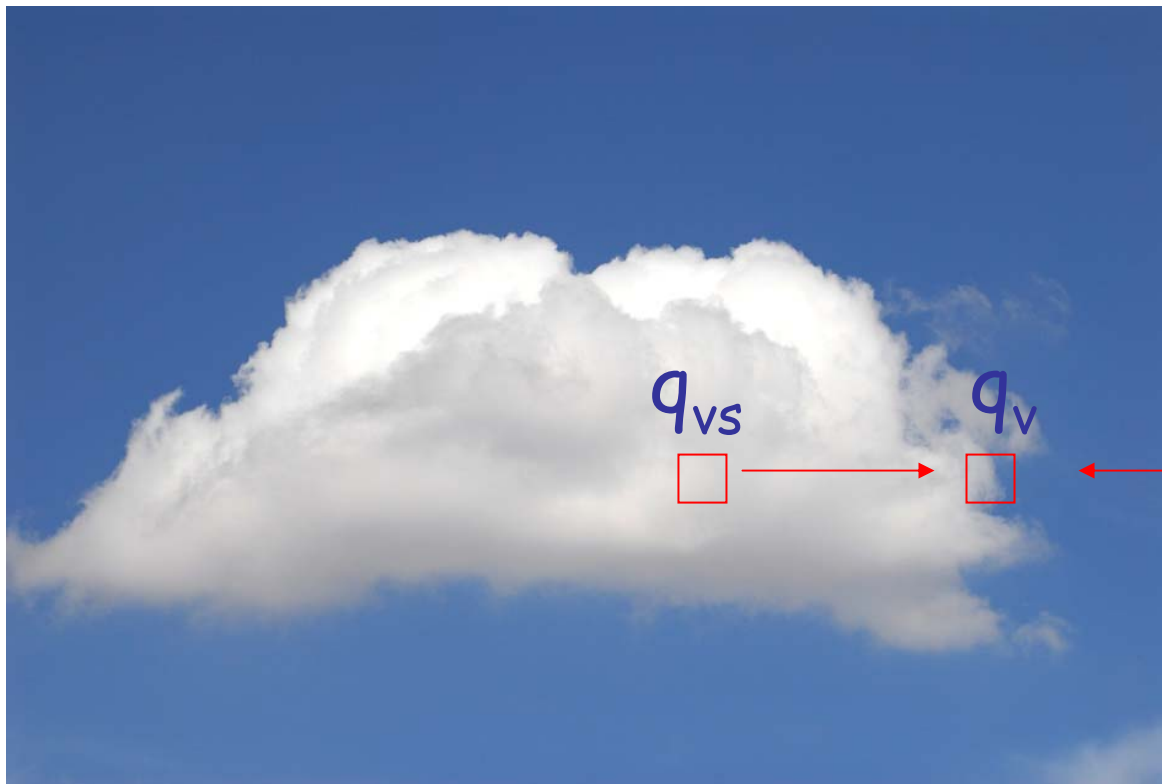
$$\lambda_0 \leq \lambda \leq \Lambda \quad C = \underline{\beta} C^{\text{a}} \quad (\text{adiabatic})$$

$\beta$  - fraction of the gridbox covered by cloudy air

$$C^{\text{a}} = -\frac{dq_{vs}}{dt} \quad - \text{adiabatic condensation rate}$$

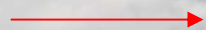
# $\beta$ diagnosed

Grabowski (2007) proposed diagnostic formula for  $\beta$  based on the relative humidity of a gridbox and on the environmental relative humidity at a given level.



Environmental profile

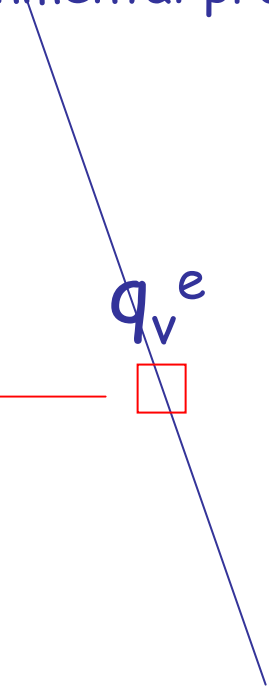
$q_{vs}$



$q_v$



$q_v^e$



# $\beta$ diagnosed

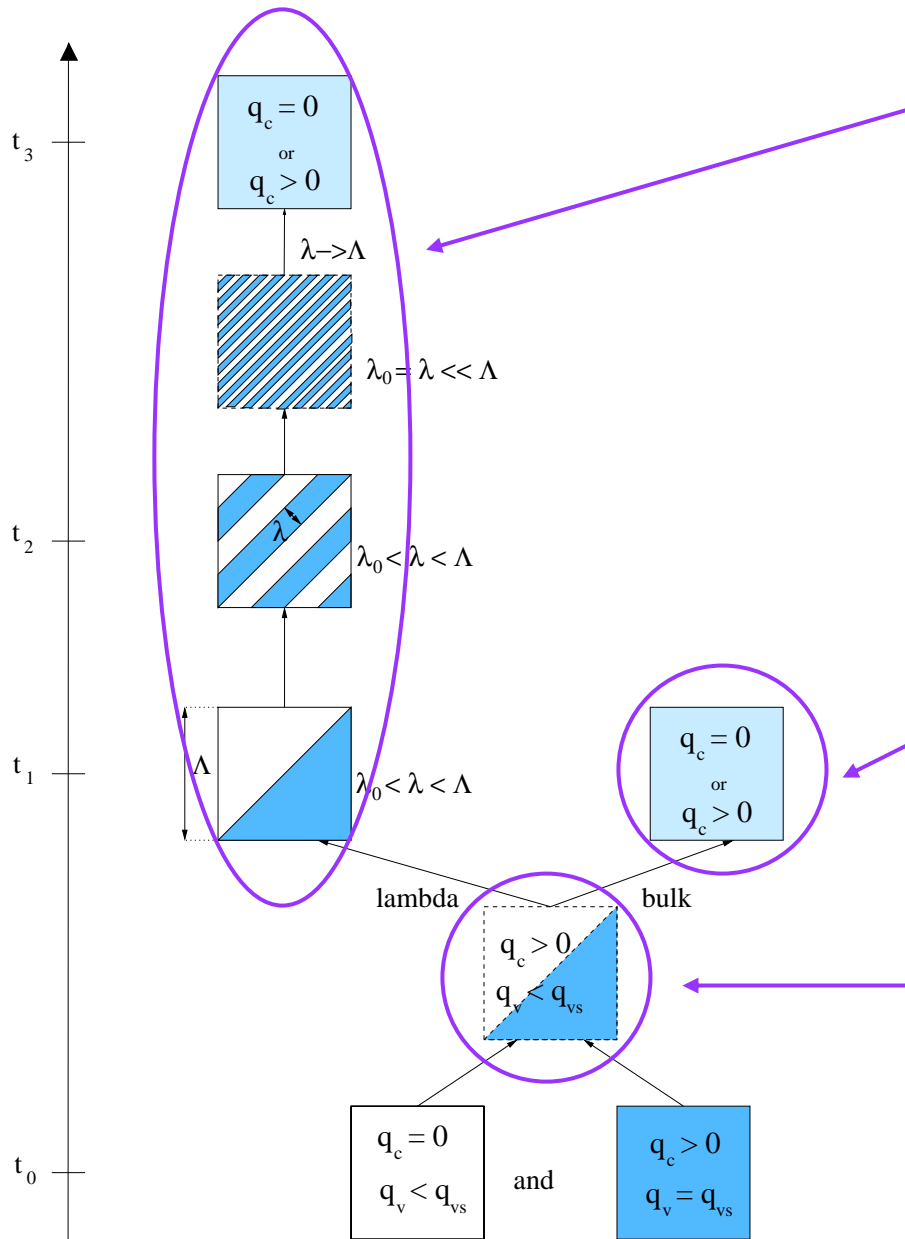
$$RH \approx \beta + (1 - \beta)RH^e$$

$$\beta = \max \left( 0, \min \left( 1, \frac{RH - RH^e}{1 - RH^e} \right) \right)$$

$RH$  - relative humidity of the gridbox

$RH^e$  - environmental relative humidity at this level

# Delay in saturation adjustment



Modified model with  $\lambda$  approach:  
 homogenization delayed until turbulent stirring reduces the filament width  $\lambda$  to the value corresponding to the microscale homogenization  $\lambda_0$

Bulk model:  
 immediate homogenization

mixing event

# Simulation of shallow convection observed in BOMEX experiment.

- 1 km deep trade wind convection layer overlays a 0.5 km deep mixed layer near the ocean surface and is covered by 0.5 km deep trade wind inversion layer.

- The cloud cover is about 10%.

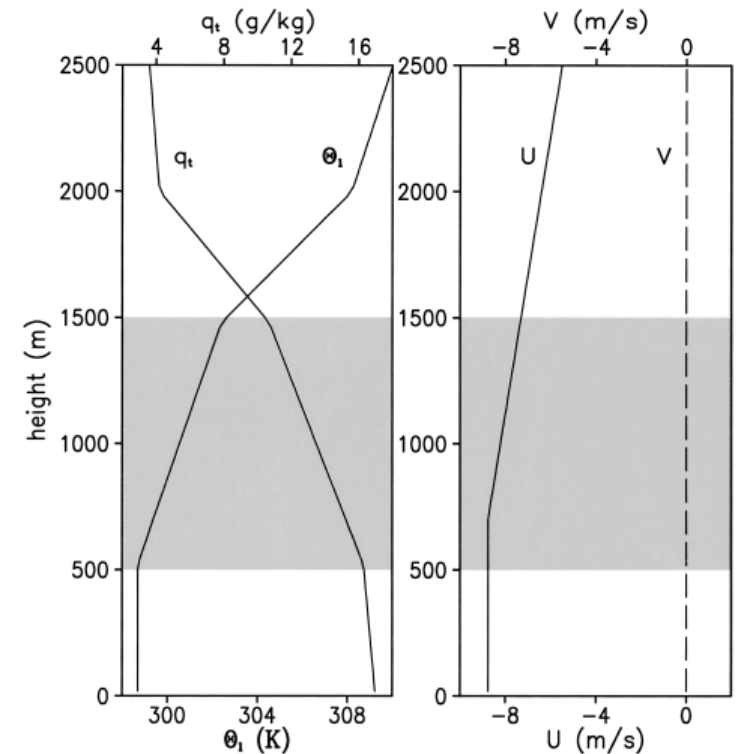


FIG. 1. Initial profiles of the total water specific humidity  $q_t$ , the liquid water potential temperature  $\theta_t$ , and the horizontal wind components  $u$  and  $v$ . The shaded area denotes the conditionally unstable cloud layer.

# Model setup

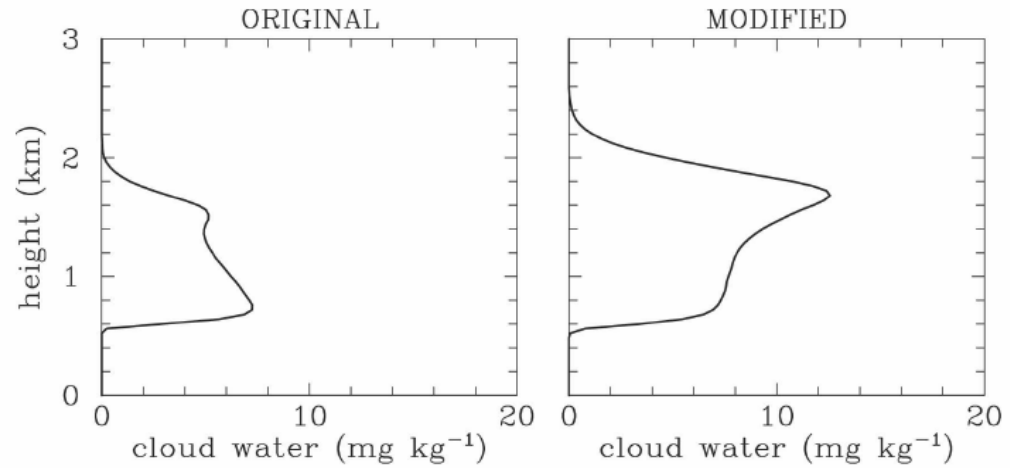
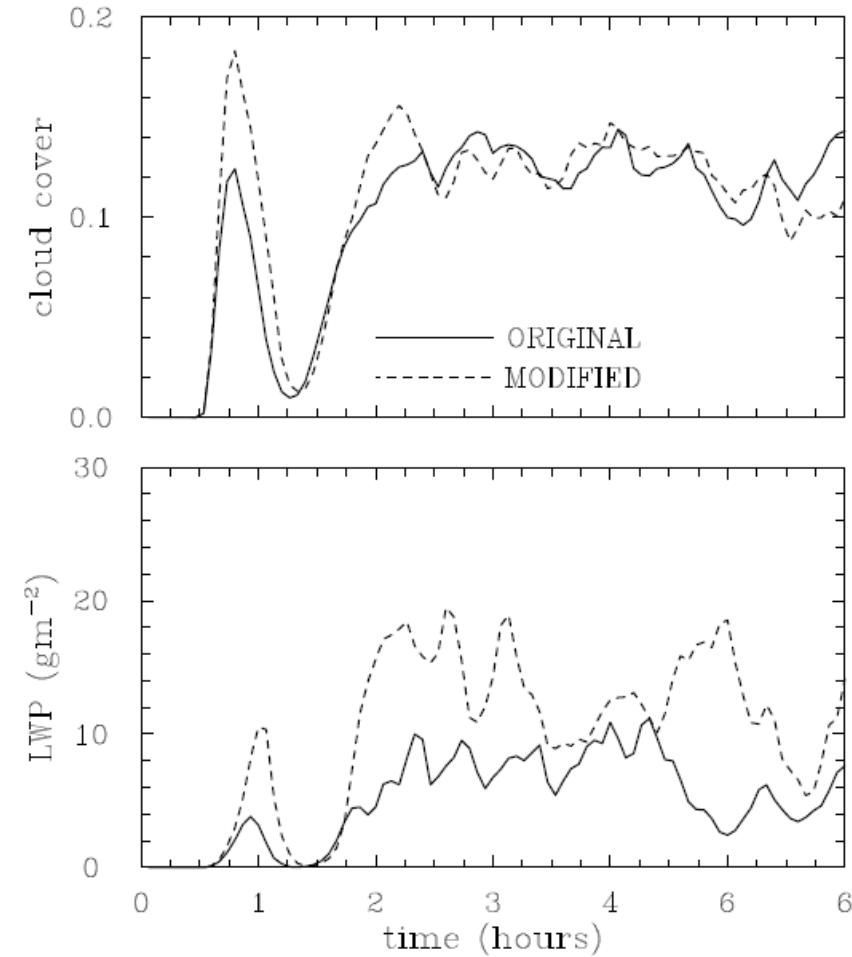
Model setup is as described in *Siebesma et al., JAS 2003* but applying different domain sizes and model gridlengths (i.e., the same number of gridpoints in the horizontal  $128 \times 128$ , 3-km vertical extent of the domain).

Three different model gridlengths were considered:

- 100m / 40m (i.e., as in Siebesma et al.)
- 50m / 40m
- 25m / 25m



# Comparison between original and modified model in *Grabowski JAS 2007*



Gridlength: 100m / 40m

# $\beta$ diagnosed

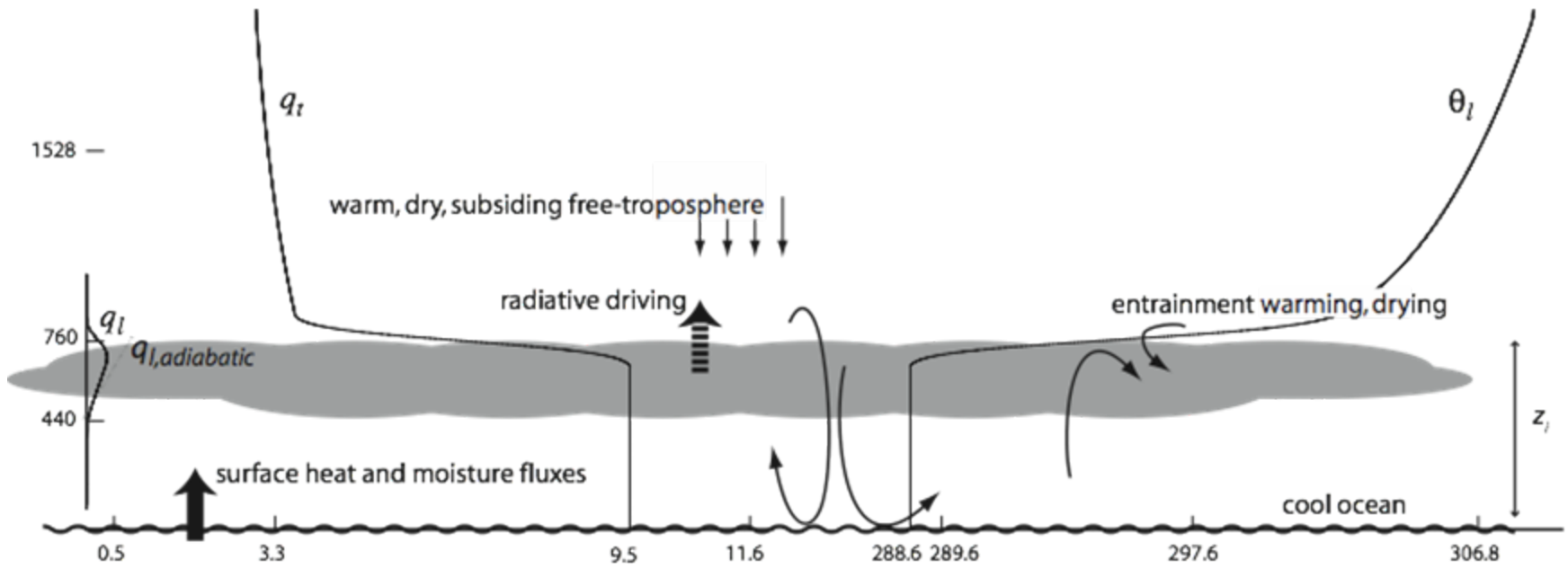
Grabowski (2007) proposed diagnostic formula for  $\beta$  based on the relative humidity of a gridbox and on the environmental relative humidity at a given level.

$$\beta = \max \left( 0, \min \left( 1, \frac{RH - RH^e}{1 - RH^e} \right) \right)$$

RH - relative humidity of the gridbox

$RH^e$  - environmental relative humidity at this level

For stratocumulus, cloud-environment mixing takes place primarily at the cloud top, where environmental profiles change rapidly.



# $\beta$ predicted

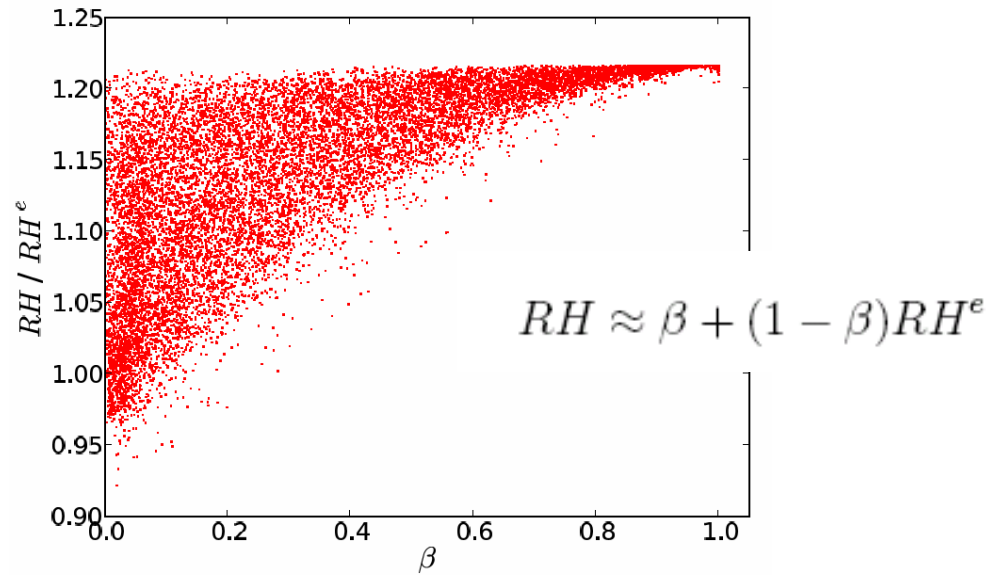
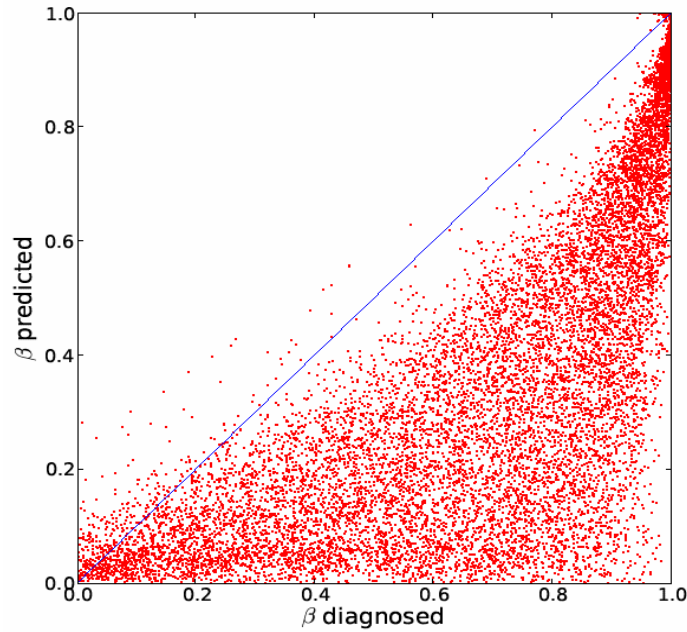
We propose to use a prognostic equation for  $\beta$  and check *a posteriori* if the diagnostic formula is accurate for shallow convection:

$$\frac{\partial \beta}{\partial t} + \frac{1}{\rho_o} \nabla \cdot (\rho_o \mathbf{u} \beta) = S_\beta + D_\beta$$

$S_\beta$  - source/sink source

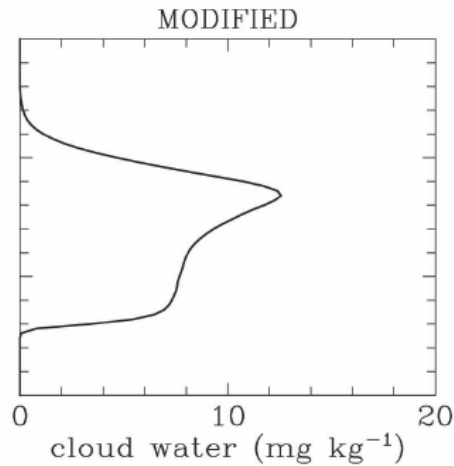
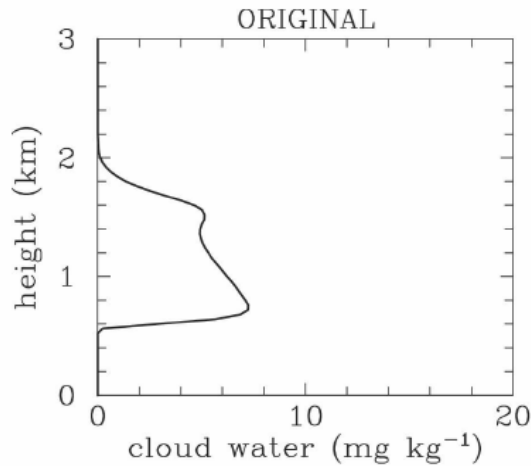
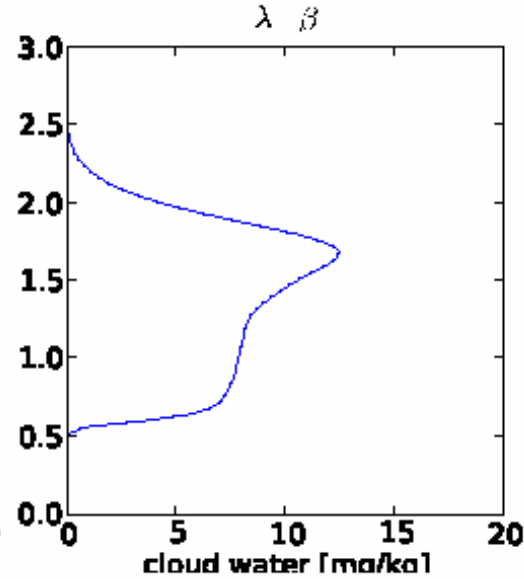
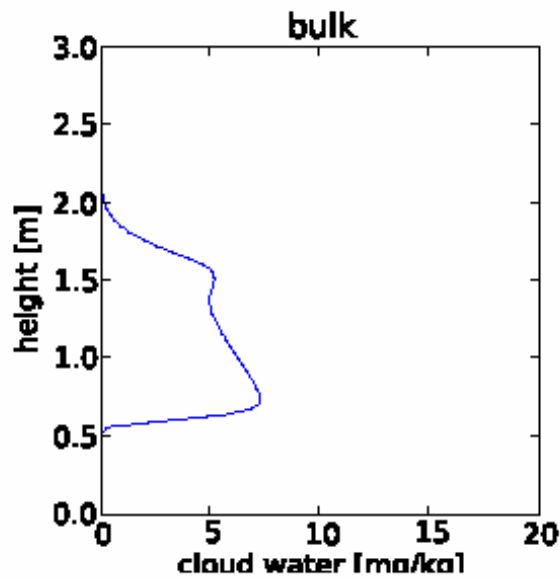
$D_\beta$  - subgrid transport term

# Comparison of predicted and diagnosed $\beta$



- The values predicted by the model are typically smaller than those diagnosed.
- The entrained air is typically more humid than far-environmental air at this level.

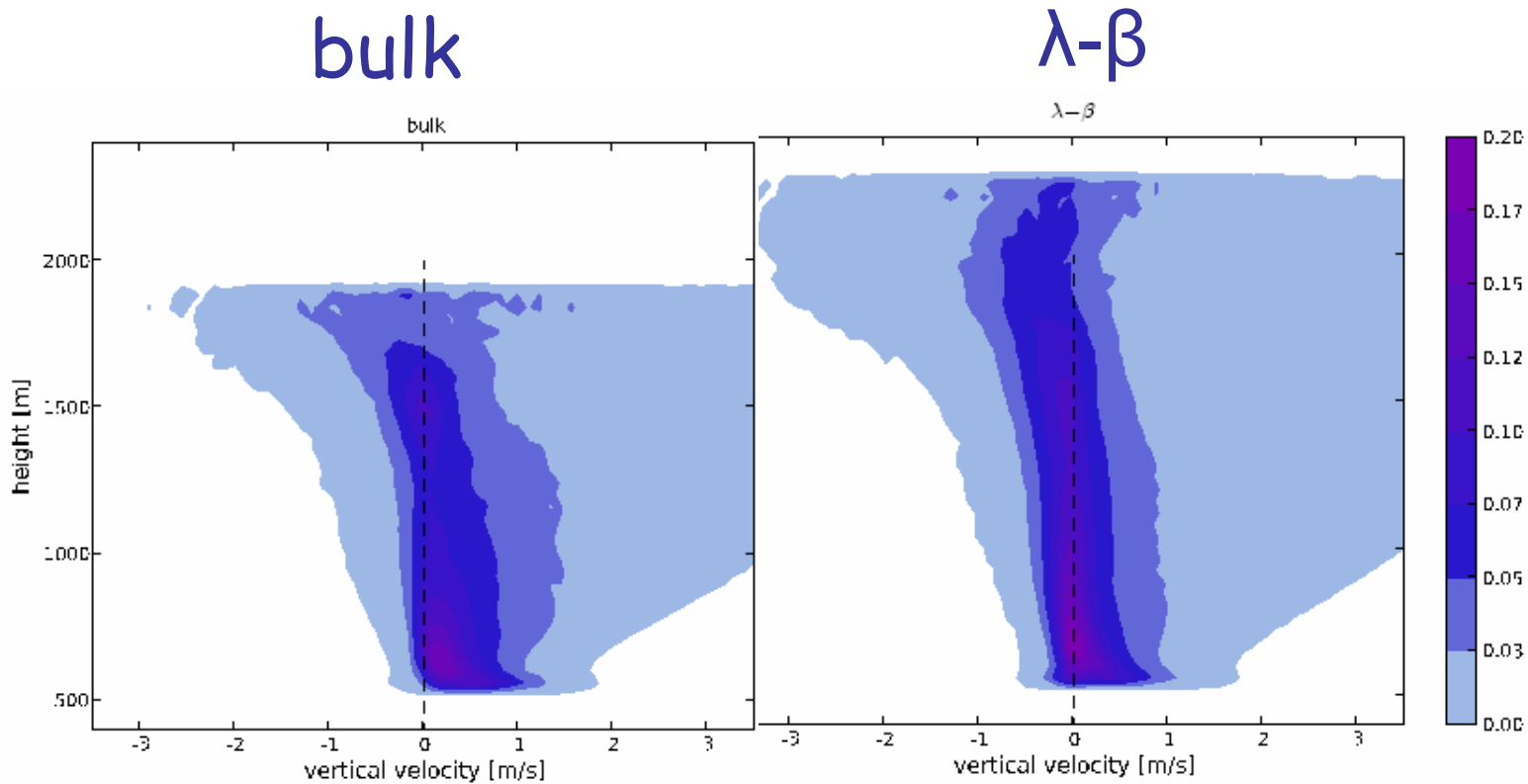
# Comparison between modified models



Differences?

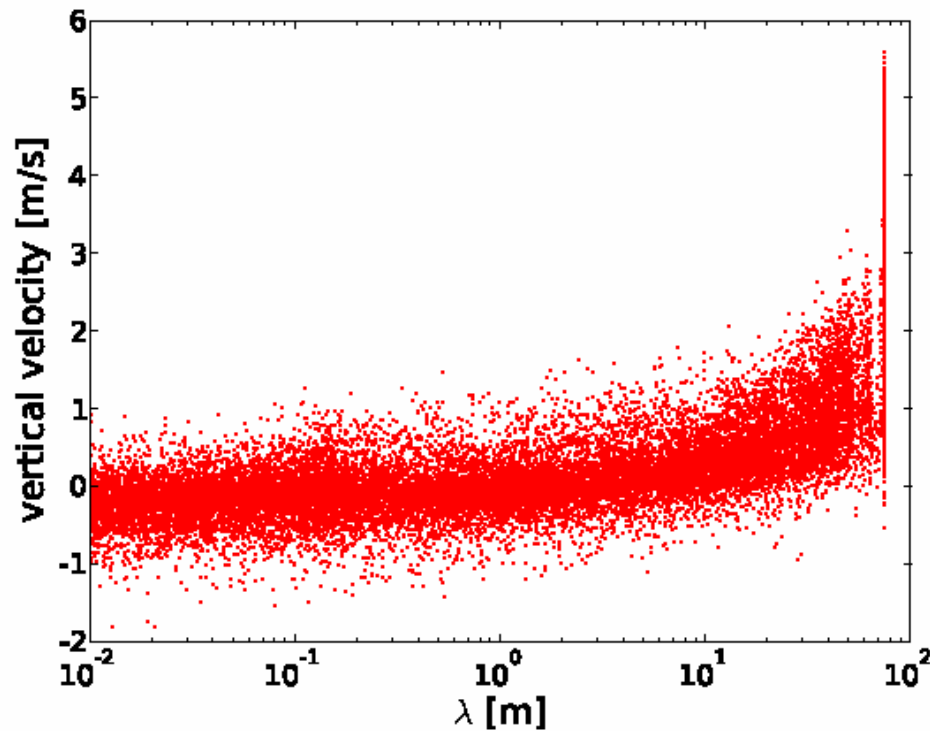
# Comparison of vertical velocities in cloud

## Countoured Frequency by Altitude Diagrams



Gridlength – 100m / 40m

# Vertical velocity versus $\lambda$



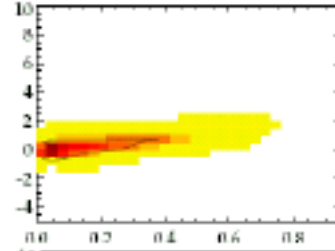
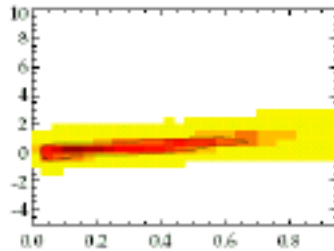
The grid boxes with intermediate values of  $\lambda$  are characterized by small positive and negative vertical velocities.



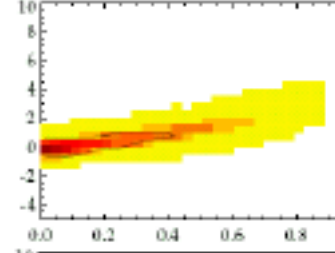
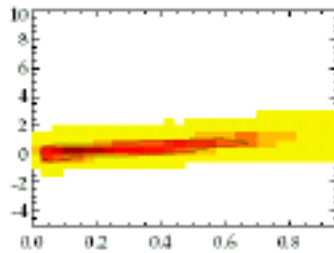
# Vertical velocity versus Adiabatic Fraction (AF) -comparison of models

bulk

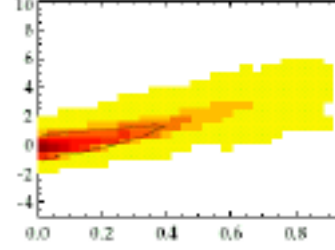
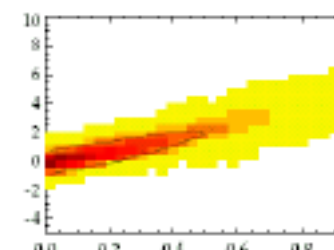
$\lambda$ - $\beta$



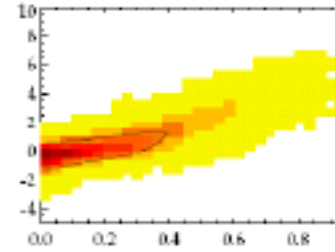
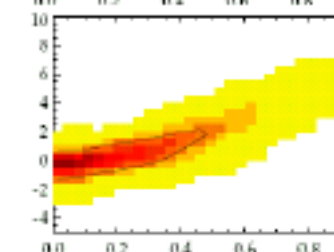
0 – 300 m



300 – 600 m



600 – 900 m



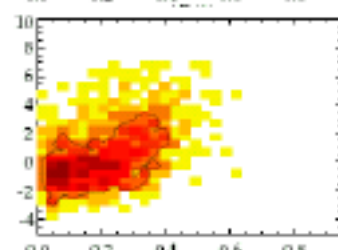
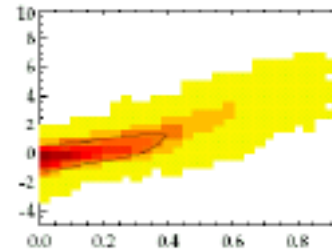
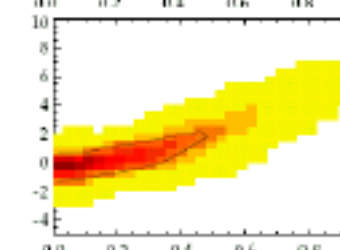
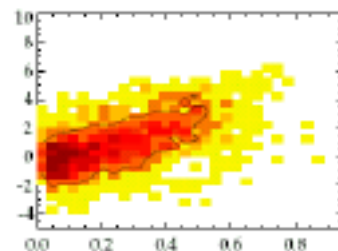
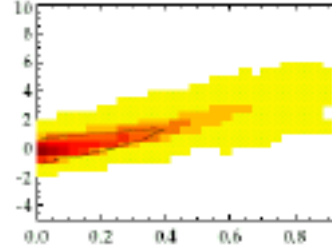
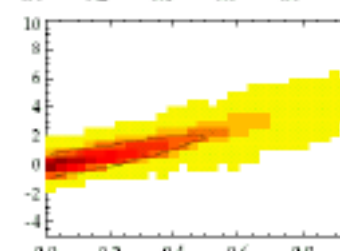
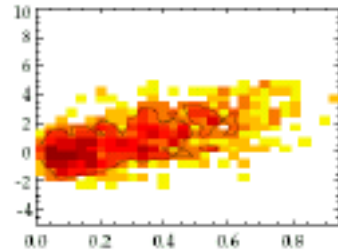
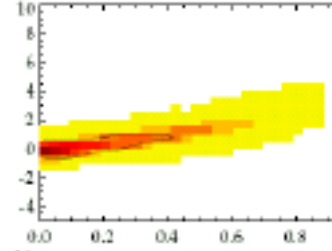
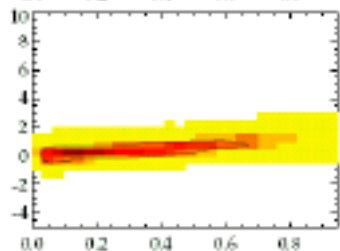
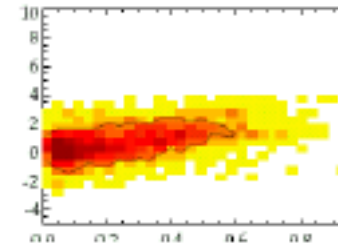
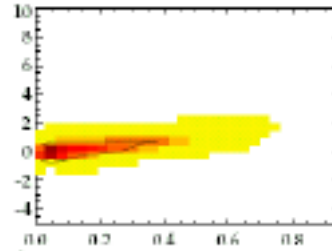
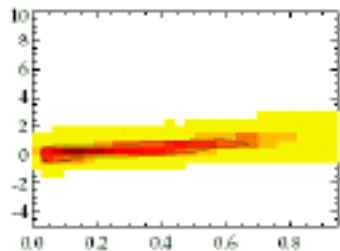
900 – 1200 m

# Vertical velocity versus Adiabatic Fraction (AF) -comparison with RICO experiment

bulk

$\lambda$ - $\beta$

RICO experiment



# Summary

- Including  $\lambda$  parameter in the bulk model allows representing in a simple way progress of turbulent mixing between cloudy air and entrained dry environmental air
- $\beta$  should be another model variable

# Future plans

- Use  $\lambda$  approach in a model with more complicated microphysics (a double-moment bulk scheme) to predict changes of the mean size of cloud droplets.
- Apply  $\lambda$  approach to stratocumulus cases.
- Compare model result with experimental data from RICO, IMPACT campaign.